E01 – Interpolation

NAG Fortran Library Routine Document E01BGF

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of **bold italicised** terms and other implementation-dependent details.

1 Purpose

E01BGF evaluates a piecewise cubic Hermite interpolant and its first derivative at a set of points.

2 Specification

```
SUBROUTINE E01BGF(N, X, F, D, M, PX, PF, PD, IFAIL) INTEGER N, M, IFAIL real X(N), F(N), D(N), PX(M), PF(M), PD(M)
```

3 Description

This routine evaluates a piecewise cubic Hermite interpolant, as computed by E01BEF, at the points PX(i), for i = 1, 2, ..., m. The first derivatives at the points are also computed. If any point lies outside the interval from X(1) to X(N), values of the interpolant and its derivative are extrapolated from the nearest extreme cubic, and a warning is returned.

If values of the interpolant only, and not of its derivative, are required, E01BFF should be used.

The routine is derived from routine PCHFD in Fritsch (1982).

4 References

Fritsch F N (1982) PCHIP final specifications *Report UCID-30194* Lawrence Livermore National Laboratory

5 Parameters

1:	N – INTEGER	Input
2:	X(N) - real array	Input
3:	F(N) - real array	Input
4:	D(N) - real array	Input

On entry: N, X, F and D must be unchanged from the previous call of E01BEF.

5: M - INTEGER Input

On entry: m, the number of points at which the interpolant is to be evaluated.

Constraint: M > 1.

6: PX(M) - real array Input

On entry: the m values of x at which the interpolant is to be evaluated.

7: PF(M) - real array Output On exit: PF(i) contains the value of the interpolant evaluated at the point PX(i), for i = 1, 2, ..., m.

8: PD(M) - real array

Output

On switt PD(i) contains the first derivative of the interpolant evaluated at the point PV(i) for

On exit: PD(i) contains the first derivative of the interpolant evaluated at the point PX(i), for i = 1, 2, ..., m.

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9: IFAIL – INTEGER

Input/Output

On entry: IFAIL must be set to 0, -1 or 1. Users who are unfamiliar with this parameter should refer to Chapter P01 for details.

On exit: IFAIL = 0 unless the routine detects an error (see Section 6).

For environments where it might be inappropriate to halt program execution when an error is detected, the value -1 or 1 is recommended. If the output of error messages is undesirable, then the value 1 is recommended. Otherwise, for users not familiar with this parameter the recommended value is 0. When the value -1 or 1 is used it is essential to test the value of IFAIL on exit.

6 Error Indicators and Warnings

If on entry IFAIL = 0 or -1, explanatory error messages are output on the current error message unit (as defined by X04AAF).

Errors or warnings detected by the routine:

```
IFAIL = 1
```

On entry, N < 2.

IFAIL = 2

The values of X(r), for r = 1, 2, ..., N, are not in strictly increasing order.

IFAIL = 3

On entry, M < 1.

IFAIL = 4

At least one of the points PX(i), for i = 1, 2, ..., M, lies outside the interval [X(1), X(N)], and extrapolation was performed at all such points. Values computed at these points may be very unreliable.

7 Accuracy

The computational errors in the arrays PF and PD should be negligible in most practical situations.

8 Further Comments

The time taken by the routine is approximately proportional to the number of evaluation points, m. The evaluation will be most efficient if the elements of PX are in non-decreasing order (or, more generally, if they are grouped in increasing order of the intervals [X(r-1),X(r)]). A single call of E01BGF with m>1 is more efficient than several calls with m=1.

9 Example

This example program reads in values of N, X, F and D, and calls E01BGF to compute the values of the interpolant and its derivative at equally spaced points.

9.1 Program Text

Note: the listing of the example program presented below uses *bold italicised* terms to denote precision-dependent details. Please read the Users' Note for your implementation to check the interpretation of these terms. As explained in the Essential Introduction to this manual, the results produced may not be identical for all implementations.

```
* E01BGF Example Program Text

* Mark 14 Revised. NAG Copyright 1989.

* .. Parameters ..
INTEGER NIN, NOUT
PARAMETER (NIN=5,NOUT=6)
```

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```
INTEGER
                      MMAX, NMAX
     PARAMETER
                      (MMAX=21,NMAX=50)
     .. Local Scalars ..
                       STEP
     INTEGER
                       I, IFAIL, M, N, R
      .. Local Arrays ..
     real
                       D(NMAX), F(NMAX), PD(MMAX), PF(MMAX), PX(MMAX),
                       X(NMAX)
      .. External Subroutines ..
     EXTERNAL
                     E01BGF
      .. Intrinsic Functions ..
     INTRINSIC
                     MIN
      .. Executable Statements ..
     WRITE (NOUT,*) 'E01BGF Example Program Results'
     Skip heading in data file
     READ (NIN,*)
     READ (NIN,*) N
     IF (N.GT.O .AND. N.LE.NMAX) THEN
        DO 20 R = 1, N
           READ (NIN, \star) X(R), F(R), D(R)
  20
         CONTINUE
         READ (NIN,*) M
         IF (M.GT.O .AND. M.LE.MMAX) THEN
           Compute M equally spaced points from X(1) to X(N).
           STEP = (X(N)-X(1))/(M-1)
           DO 40 I = 1, M
              PX(I) = MIN(X(1)+(I-1)*STEP,X(N))
           CONTINUE
  40
           IFAIL = 0
            CALL EO1BGF(N,X,F,D,M,PX,PF,PD,IFAIL)
           WRITE (NOUT, *)
           WRITE (NOUT, *)
                                 Interpolated
                                               Interpolated'
           WRITE (NOUT, *)
                                        Value
                   Abscissa
                                                 Derivative'
           DO 60 I = 1, M
              WRITE (NOUT, 99999) PX(I), PF(I), PD(I)
  60
            CONTINUE
        END IF
     END IF
     STOP
99999 FORMAT (1X,2F15.4,1P,e15.3)
     END
```

9.2 Program Data

9.3 Program Results

E01BGF Example Program Results

	Interpolated	Interpolated
Abscissa	Value	Derivative
7.9900	0.0000	0.000E+00
9.1910	0.4640	6.060E-01

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10.3920	0.9645	4.569E-02
11.5930	0.9965	9.917E-03
12.7940	0.9992	6.249E-04
13.9950	0.9998	2.708E-04
15.1960	0.9999	2.809E-05
16.3970	1.0000	2.034E-05
17.5980	1.0000	1.308E-05
18.7990	1.0000	6.297E-06
20.0000	1.0000	-9.529E-22

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