NAG Fortran Library Routine Document D06BAF

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of **bold italicised** terms and other implementation-dependent details.

1 Purpose

D06BAF generates a boundary mesh on a closed connected subdomain Ω of \mathbb{R}^2 .

2 Specification

```
SUBROUTINE DO6BAF(NLINES, COORCH, LINE, FBND, COORUS, NUS, RATE, NCOMP,
                   NLCOMP, LCOMP, NVMAX, NEDMX, NVB, COOR, NEDGE, EDGE,
2
                   ITRACE, RUSER, IUSER, RWORK, LRWORK, IWORK, LIWORK,
3
                   NLINES, LINE(4, NLINES), NUS, NCOMP, NLCOMP(NCOMP),
INTEGER
                   LCOMP(NLINES), NVMAX, NEDMX, NVB, NEDGE,
                   EDGE(3,NEDMX), ITRACE, IUSER(*), LRWORK,
2
                   IWORK(LIWORK), LIWORK, IFAIL
3
real
                   COORCH(2,NLINES), FBND, COORUS(2,NUS), RATE(NLINES),
                   COOR(2,NVMAX), RUSER(*), RWORK(LRWORK)
1
 EXTERNAL
                   FBND
```

3 Description

Given a closed connected subdomain Ω of \mathbb{R}^2 , whose boundary $\partial\Omega$ is divided by characteristic points into m distinct line segments, D06BAF generates a boundary mesh on $\partial\Omega$. Each line segment may be a straight line, a curve defined by the equation f(x,y)=0, or a polygonal curve defined by a set of given boundary mesh points.

This routine is primarily designed for use with either D06AAF (a simple incremental method) or D06ABF (Delaunay–Voronoi method) or D06ACF (Advancing Front method) to triangulate the interior of the domain Ω . For more details about the boundary and interior mesh generation, consult the D06 Chapter Introduction as well as George and Borouchaki (1998).

This routine is derived from material in the MODULEF package from INRIA (Institut National de Recherche en Informatique et Automatique).

4 References

George P L and Borouchaki H (1998) Delaunay Triangulation and Meshing: Application to Finite Elements Editions HERMES, Paris

5 Parameters

1: NLINES – INTEGER

Input

On entry: m, the number of lines that define the boundary of the closed connected subdomain (this equals the number of characteristic points which separate the entire boundary $\partial \Omega$ into lines).

Constraint: NLINES ≥ 1 .

2: COORCH(2,NLINES) – *real* array

Input

On entry: COORCH(1,i) contains the x-coordinate of the ith characteristic point, for i = 1, ..., NLINES; while COORCH(2,i) contains the corresponding y-coordinate.

3: LINE(4,NLINES) – INTEGER array

Input

On entry: the description of the lines that define the boundary domain. The line i, for i = 1, ..., m, is defined as follows:

- (a) LINE(1, i): the number of points on the line, including two end-points.
- (b) LINE(2, i): the first end-point of the line. If LINE(2, i) = j, then the coordinates of the first end-point are those stored in COORCH(:, j).
- (c) LINE(3, i): the second end-point of the line. If LINE(3, i) = k, then the coordinates of the second end-point are those stored in COORCH(:, k).
- (d) LINE(4, i): this defines the type of line segment connecting the end-points. Additional information is conveyed by the numerical value of LINE(4, i) as follows:
 - (i) LINE(4,i) > 0, the line is described in the user-supplied function FBND with LINE(4,i) as the index. In this case, the line must be described in the trigonometric (anticlockwise) direction;
 - (ii) LINE(4, i) = 0, the line is a straight line;
 - (iii) if LINE(4, i) < 0, say (-p), then the line is a polygonal arc joining the end-points and interior points specified in COORUS. In this case the line contains the points whose coordinates are stored in COORCH(:, j), COORUS(:, p), COORUS(:, p+1), . . . , COORUS(:, p+r-3), COORCH(:, k), where r=LINE(1,i), j=LINE(2,i) and k=LINE(3,i).

Constraints:

```
2 \le LINE(1,i);

1 \le LINE(2,i) \le NLINES;

1 \le LINE(3,i) \le NLINES;

LINE(2,i) \ne LINE(3,i), \text{ for } i = 1,..., NLINES.
```

For each line described by the user-supplied function (lines with LINE(4, i) > 0, i = 1, ..., NLINES) the two end-points (LINE(2, i) and LINE(3, i)) lie on the curve defined by index LINE(4, i) in the user-supplied function FBND, i.e.

FBND(LINE(4, i), COORCH(1, LINE(2, i)), COORCH(2, LINE(2, i)), RUSER, IUSER) = 0 and FBND(LINE(4, i), COORCH(1, LINE(3, i)), COORCH(2, LINE(3, i)), RUSER, IUSER) = 0, for i = 1, ..., NLINES.

For all lines described as polygonal arcs (lines with LINE(4, i) < 0, $i = 1, \ldots, \text{NLINES}$) the sets of intermediate points (i.e. [-LINE(4, i) : -LINE(4, i) + LINE(1, i) - 3] for all i such that LINE(4, i) < 0) are not overlapping. This can be expressed as:

$$-\mathsf{LINE}(4,i) + \mathsf{LINE}(1,i) - 3 = \sum_{\{i, \mathsf{LINE}(4,i) < 0\}} \{\mathsf{LINE}(1,i) - 2\}$$

or

$$-LINE(4, i) + LINE(1, i) - 2 = -LINE(4, j),$$

for a j such that j = 1, ..., NLINES, $j \neq i$ and LINE(4, j) < 0.

4: FBND – *real* FUNCTION, supplied by the user.

External Procedure

This function must be supplied by the user to calculate the value of the function which describes the curve $\{(x,y)\in\mathbb{R}^2;$ such that $f(x,y)=0\}$ on segments of the boundary for which LINE(4,i)>0. If there are no boundaries for which LINE(4,i)>0 FBND will never be referenced by D06BAF and FBND may be the dummy function D06BAD. (D06BAD is included in the NAG Fortran Library and so need not be supplied by the user. Its name may be implementation-dependent: see the Users' Note for your implementation for details.)

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Its specification is:

1: I – INTEGER Input

On entry: LINE(4, i), the reference index of the line (portion of the contour) i described.

2: X - real Input

3: Y - real Input

On entry: the values of x and y at which f(x,y) is to be evaluated.

4: RUSER(*) – *real* array *Input*

5: IUSER(*) – INTEGER array

Input

On entry: the user is free to use these arrays to supply information to this function from the calling (sub)program.

FBND must be declared as EXTERNAL in the (sub)program from which D06BAF is called. Parameters denoted as *Input* must **not** be changed by this procedure.

5: COORUS(2,NUS) – *real* array

Input

On entry: the coordinates of the intermediate points for polygonal arc lines. For a line i defined as a polygonal arc (i.e., LINE(4, i) < 0), if p = -LINE(4, i), then COORUS(1, k), $k = p, p + 1, \ldots, p + \text{LINE}(1, i) - 3$ must contain the x-coordinate of the consecutive intermediate points for this line. Similarly COORUS(2, k), $k = p, p + 1, \ldots, p + \text{LINE}(1, i) - 3$ must contain the corresponding y-coordinate.

6: NUS – INTEGER Input

On entry: the second dimension of the array COORUS as declared in the (sub)program from which D06BAF is called.

Constraint: NUS $\geq \sum_{\{i,\text{LINE}(4,i)<0\}} \{\text{LINE}(1,i)-2\}.$

7: RATE(NLINES) – *real* array

Input

On entry: RATE(i) is the geometric progression ratio between the points to be generated on the line i, for i = 1, ..., m and LINE(4, i) ≥ 0 . RATE(i) is not referenced if LINE(4, i) < 0.

Constraint: RATE(i) > 0; for i = 1, ..., NLINES and LINE(4, i) ≥ 0 .

8: NCOMP – INTEGER

Input

On entry: n, the number of separately connected components of the boundary.

Constraint: $NCOMP \ge 1$.

9: NLCOMP(NCOMP) – INTEGER array

Input

On entry: |NLCOMP(k)| is the number of line segments in component k of the contour. The line i of component k runs in the direction LINE(2,i) to LINE(3,i) if NLCOMP(k) > 0, and in the opposite direction otherwise; for $k = 1, \ldots, n$.

Constraint:

 $1 \le |\text{NLCOMP}(k)| \le \text{NLINES}, \text{ for } k = 1, \dots, \text{NCOMP},$

$$\sum_{k=1}^{n} |\text{NLCOMP}(k)| = \text{NLINES}.$$

10: LCOMP(NLINES) - INTEGER array

Input

On entry: LCOMP(l1:l2), where $l2 = \sum_{i=1}^{k} |\text{NLCOMP}(i)|$ and l1 = l2 + 1 - |NLCOMP(k)| is the list of line numbers for the kth components of the boundary, for $k = 1, \ldots, \text{NCOMP}$.

Constraint: LCOMP must hold a valid permutation of the integers [1, NLINES].

11: NVMAX – INTEGER

Input

On entry: the maximum number of the boundary mesh vertices to be generated.

Constraint: NVMAX > NLINES.

12: NEDMX – INTEGER

Input

On entry: the maximum number of boundary edges in the boundary mesh to be generated.

Constraint: NEDMX ≥ 1 .

13: NVB – INTEGER

Output

On exit: the total number of boundary mesh vertices generated.

14: COOR(2,NVMAX) – *real* array

Output

On exit: COOR(1, i) will contain the x-coordinate of the ith boundary mesh vertex generated, for i = 1, ..., NVB; while COOR(2, i) will contain the corresponding y-coordinate.

15: NEDGE – INTEGER

Output

On entry: the total number of boundary edges in the boundary mesh.

16: EDGE(3,NEDMX) – INTEGER array

Output

On exit: the specification of the boundary edges. EDGE(1:2,j) will contain the vertex number of the two end-points of the jth boundary edge. EDGE(3,j) is a reference number for the jth boundary edge and

EDGE(3, j) = LINE(4, i), where i and j are such that the jth edges is part of the ith line of the boundary and $LINE(4, i) \ge 0$;

EDGE(3, j) = 100 + |LINE(4, i)|, where i and j are such that the jth edges is part of the ith line of the boundary and LINE(4, i) < 0.

17: ITRACE – INTEGER

Input

On entry: the level of trace information required from D06BAF as follows:

if ITRACE < 0, no output is generated.

if ITRACE = 1, then output from the boundary mesh generator is printed on the current advisory message unit (see X04ABF). This output contains the input informations of each line and each connected component of the boundary.

if ITRACE > 1, then the output is similar to that produced when ITRACE = 1, but the coordinates of the generated vertices on the boundary are also output.

if ITRACE = -1, then an analysis of the output boundary mesh is printed on the current advisory message unit. This analysis includes the orientation (clockwise or anticlockwise) of each connected component of the boundary. Those informations could be of interest to the user, especially if an interior meshing is carried out using the output of this routine, calling either D06AAF, D06ABF or D06ACF.

Users are advised to set ITRACE = 0, unless they are experienced with Finite Element meshes generation.

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18: RUSER(*) – *real* array

Input

Note: the dimension of the array RUSER must be at least 1.

On entry: the user is free to use these arrays to supply information to the user-supplied function FBND from the calling (sub)program.

19: IUSER(*) – INTEGER array

Input

Note: the dimension of the array IUSER must be at least 1.

20: RWORK(LRWORK) - real array

Workspace

21: LRWORK – INTEGER

Input

On entry: the dimension of the array RWORK as declared in the (sub)program from which D06BAF is called.

Constraint: LRWORK $\geq 2 \times (\text{NLINES} + \text{NUS}) + 2 \times \max_{i=1,...,m} \{\text{LINE}(1,i)\} \times \text{NLINES}.$

22: IWORK(LIWORK) - INTEGER array

Workspace

23: LIWORK – INTEGER

Input

On entry: the dimension of the array IWORK as declared in the (sub)program from which D06BAF is called.

$$\textit{Constraint}: \ \text{LIWORK} \geq \sum_{\{i, \text{LINE}(4, i) < 0\}} \ \{ \text{LINE}(1, i) - 2 \} + 8 \times \text{NLINES} + \text{NVMAX} + 3 \times 10^{-5} \text{MeV} + 10^{-5} \text{$$

 $NEDMX + 2 \times NUS$.

24: IFAIL – INTEGER

Input/Output

On entry: IFAIL must be set to 0, -1 or 1. Users who are unfamiliar with this parameter should refer to Chapter P01 for details.

On exit: IFAIL = 0 unless the routine detects an error (see Section 6).

For environments where it might be inappropriate to halt program execution when an error is detected, the value -1 or 1 is recommended. If the output of error messages is undesirable, then the value 1 is recommended. Otherwise, for users not familiar with this parameter the recommended value is 0. When the value -1 or 1 is used it is essential to test the value of IFAIL on exit.

6 Error Indicators and Warnings

If on entry IFAIL = 0 or -1, explanatory error messages are output on the current error message unit (as defined by X04AAF).

Errors or warnings detected by the routine:

```
IFAIL = 1
```

```
On entry, NLINES < 1;
               NVMAX < NLINES;
or
               NEDMX < 1;
or
               NCOMP < 1;
or
               LRWORK < 2 \times (\text{NLINES} + \text{NUS}) + 2 \times \max_{i=1}^{m} \{\text{LINE}(1, i)\} \times \text{NLINES};
or
or
\begin{aligned} & \text{LIWORK} < \sum_{\{i, \text{LINE}(4, i) < 0\}} \{ \text{LINE}(1, i) - 2 \} + 8 \times \text{NLINES} + \text{NVMAX} + 3 \times \text{NEDMX} + 2 \times \text{NUS}; \\ & \text{or} & & \text{NUS} < \sum_{\{i, \text{LINE}(4, i) < 0\}} \{ \text{LINE}(1, i) - 2 \}; \end{aligned}
               RATE(i) < 0.0 for some i = 1, ..., NLINES with LINE(4, i) > 0;
or
               LINE(1, i) < 2 for some i = 1, ..., NLINES;
or
               LINE(2, i) < 1 or LINE(2, i) > NLINES for some i = 1, ..., NLINES;
or
```

```
LINE(3, i) < 1 or LINE(3, i) > NLINES for some i = 1, ..., NLINES;
or
          LINE(2, i) = LINE(3, i) for some i = 1, ..., NLINES;
or
          NLCOMP(k) = 0, or |NLCOMP(k)| > NLINES for a k = 1, ..., NCOMP;
or
               |NLCOMP(k)| \neq NLINES;
or
          LCOMP does not represent a valid permutation of the integers in [1, NLINES];
or
          one of the end-points for a line i described by the user-supplied function (lines with
or
          LINE(4,i) > 0, for i = 1, \dots, NLINES) does not belong to the corresponding curve in
          the user-supplied function FBND;
          the intermediate points for the lines described as polygonal arcs (lines with LINE(i) < 0,
or
```

IFAIL = 2

An error has occurred during the generation of the boundary mesh. It appears that NEDMX is not large enough, so the user is advised to increase the value of NEDMX.

IFAIL = 3

An error has occurred during the generation of the boundary mesh. It appears that NVMAX is not large enough, so the user is advised to increase the value of NVMAX.

IFAIL = 4

An error has occurred during the generation of the boundary mesh. Check the definition of each line (the argument LINE) and each connected component of the boundary (the arguments NLCOMP, and LCOMP, as well as the coordinates of the characteristic points. Setting ITRACE > 0 may provide more details.

7 Accuracy

Not applicable.

8 Further Comments

The boundary mesh generation technique in this routine has a 'tree' structure. The boundary should be partitioned into geometrically simple segments (straight lines or curves) delimited by characteristic points. Then, the lines should be assembled into connected component of the boundary domain.

Using this strategy, the inputs to that routine can be built up, following the requirements stated in the arguments description section:

the characteristic and the user-supplied intermediate points:

for i = 1, ..., NLINES) are overlapping.

NLINES, NUS, COORCH and COORUS;

the characteristic lines:

LINE, FBND, RATE

finally the assembly of lines into the connected components of the boundary:

NCOMP, and

NLCOMP, LCOMP.

The example below details the use of this strategy.

9 Example

The NAG logo is taken as an example of a geometry with holes. The boundary has been partioned in 40 lines characteristic points; including 4 for the exterior boundary and 36 for the logo itself. All line

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geometry specifications have been considered, see the argument description of LINE, including 4 lines defined as polygonal arc, 4 defined by a user-supplied function and all the others are straight lines.

Figure 1 top represents the boundary mesh of the NAG logo; there are 259 nodes and 259 edges. The Figure 1 middle and bottom represent the final mesh built using respectively the Delaunay-Voronoi (D06ABF) and the Advancing front (D06ACF) method.

9.1 Program Text

Note: the listing of the example program presented below uses **bold italicised** terms to denote precision-dependent details. Please read the Users' Note for your implementation to check the interpretation of these terms. As explained in the Essential Introduction to this manual, the results produced may not be identical for all implementations.

```
DO6BAF Example Program Text
     Mark 20 Release. NAG Copyright 2001.
      .. Parameters ..
      INTEGER
                       NIN, NOUT
      PARAMETER
                        (NIN=5, NOUT=6)
                       NEDMX, NVMAX, NLINESX, NUS, NCOMPX, NVIMX,
     INTEGER
                       MAXCAN, LRWORK, LIWORK
     PARAMETER
                       (NEDMX=300, NVMAX=1000, NLINESX=50, NUS=100,
                        NCOMPX=5, NVIMX=20, MAXCAN=10000,
                       LRWORK=12*NVMAX+3*MAXCAN+15,
                       LIWORK=8*NEDMX+55*NVMAX+MAXCAN+78)
      .. Local Scalars ..
                       XO, XA, XB, XMAX, XMIN, YO, YMAX, YMIN I, IFAIL, ITRACE, J, K, NCOMP, NEDGE, NELT,
     real
     INTEGER
                       NLINES, NPROPA, NV, NVB, NVINT, REFTK
      CHARACTER
      .. Local Arrays ..
     real
                       COOR(2,NVMAX), COORCH(2,NLINESX), COORUS(2,NUS),
                        RATE(NLINESX), RUSER(4), RWORK(LRWORK),
                        WEIGHT (NVIMX)
                        CONN(3,2*NVMAX+5), EDGE(3,NEDMX), IUSER(1),
      TNTEGER
                        IWORK(LIWORK), LCOMP(NLINESX), LINE(4,NLINESX),
                        NLCOMP (NCOMPX)
      .. External Functions ..
     real
                       FBND
     EXTERNAL
                       FBND
      .. External Subroutines ..
     EXTERNAL DOGABF, DOGACF, DOGBAF
      .. Intrinsic Functions ..
      INTRINSIC
                       ABS
      .. Executable Statements ..
     WRITE (NOUT,*) 'DO6BAF Example Program Results'
     WRITE (NOUT, *)
      Skip heading in data file
      READ (NIN, *)
      Initialise boundary mesh inputs:
*
      the number of line and of the characteristic points of
      the boundary mesh
     READ (NIN, *) NLINES
      The ellipse boundary which envelops the NAg Logo
      the N, the A and the G
      READ (NIN,*) (COORCH(1,J),J=1,NLINES)
      READ (NIN,*) (COORCH(2,J),J=1,NLINES)
     READ (NIN, \star) (COORUS(1, J), J=1, 4)
     READ (NIN,*) (COORUS(2,J),J=1,4)
      The Lines of the boundary mesh
      READ (NIN,*) ((LINE(I,J),I=1,4),RATE(J),J=1,NLINES)
```

```
The number of connected components to the boundary
   and their informations
   READ (NIN,*) NCOMP
   J = 1
   DO 20 I = 1, NCOMP
      READ (NIN, *) NLCOMP(I)
      READ (NIN,*) (LCOMP(K),K=J,J+ABS(NLCOMP(I))-1)
      J = J + ABS(NLCOMP(I))
20 CONTINUE
   READ (NIN,*) PMESH
   Data passed to the user-supplied function
   XMIN = COORCH(1,4)
   XMAX = COORCH(1,2)
   YMIN = COORCH(2,1)
   YMAX = COORCH(2,3)
   XA = (XMAX - XMIN)/2.e0
   XB = (YMAX - YMIN)/2.e0
   XO = (XMIN + XMAX)/2.e0
   YO = (YMIN+YMAX)/2.eO
   RUSER(1) = XA
   RUSER(2) = XB
   RUSER(3) = X0
   RUSER(4) = YO
   IUSER(1) = 0
   ITRACE = -1
   Call to the boundary mesh generator
   IFAIL = 0
   CALL DO6BAF (NLINES, COORCH, LINE, FBND, COORUS, NUS, RATE, NCOMP, NLCOMP,
               LCOMP, NVMAX, NEDMX, NVB, COOR, NEDGE, EDGE, ITRACE, RUSER,
               IUSER,RWORK,LRWORK,IWORK,LIWORK,IFAIL)
   IF (PMESH.EQ.'N') THEN
      WRITE (NOUT,*) 'Boundary mesh characteristics'
      WRITE (NOUT,99999) 'NVB =', NVB
WRITE (NOUT,99999) 'NEDGE =', NEDGE
   ELSE IF (PMESH.EQ.'Y') THEN
   Output the mesh to view it using the NAG Graphics Library
      WRITE (NOUT, 99998) NVB, NEDGE
      DO 40 I = 1, NVB
         WRITE (NOUT, 99997) I, COOR(1,I), COOR(2,I)
40
      CONTINUE
      DO 60 I = 1, NEDGE
         WRITE (NOUT, 99996) I, EDGE(1,I), EDGE(2,I), EDGE(3,I)
      CONTINUE
60
      WRITE (NOUT,*) 'Problem with the printing option Y or N'
      STOP
   END IF
   Initialise mesh control parameters
   ITRACE = 0
   NPROPA = 1
   NVINT = 0
```

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```
IFAIL = 0
      Call to the 2D Delaunay-Voronoi mesh generator
      CALL DO6ABF (NVB, NVINT, NVMAX, NEDGE, EDGE, NV, NELT, COOR, CONN, WEIGHT,
                  NPROPA, ITRACE, RWORK, LRWORK, IWORK, LIWORK, IFAIL)
      IF (PMESH.EQ.'N') THEN
         WRITE (NOUT, *)
           'Complete mesh (via the 2D Delaunay-Voronoi mesh'
         WRITE (NOUT,*) 'generator) characteristics'
         WRITE (NOUT, 99999) 'NV
                                 =', NV
         WRITE (NOUT, 99999) 'NELT =', NELT
      ELSE IF (PMESH.EQ.'Y') THEN
      Output the mesh to view it using the NAG Graphics Library
         WRITE (NOUT, 99998) NV, NELT
         DO 80 I = 1, NV
            WRITE (NOUT, 99995) COOR(1,I), COOR(2,I)
   80
         CONTINUE
         REFTK = 0
         DO 100 K = 1, NELT
            WRITE (NOUT, 99994) CONN(1, K), CONN(2, K), CONN(3, K), REFTK
 100
         CONTINUE
      END IF
      Call to the 2D Advancing front mesh generator
      TFATL = 0
      CALL DOGACF (NVB, NVINT, NVMAX, NEDGE, EDGE, NV, NELT, COOR, CONN, WEIGHT,
                  ITRACE,RWORK,LRWORK,IWORK,LIWORK,IFAIL)
      IF (PMESH.EQ.'N') THEN
         WRITE (NOUT,*) 'Complete mesh (via the 2D Advancing front mesh'
         WRITE (NOUT,*) 'generator) characteristics'
         WRITE (NOUT, 99999) 'NV =', NV
         WRITE (NOUT, 99999) 'NELT =', NELT
      ELSE IF (PMESH.EQ.'Y') THEN
      Output the mesh to view it using the NAG Graphics Library
         WRITE (NOUT, 99998) NV, NELT
         DO 120 I = 1, NV
            WRITE (NOUT, 99995) COOR(1,I), COOR(2,I)
 120
         CONTINUE
         REFTK = 0
         DO 140 K = 1, NELT
            WRITE (NOUT, 99994) CONN(1,K), CONN(2,K), CONN(3,K), REFTK
 140
         CONTINUE
      END IF
      STOP
99999 FORMAT (1X,A,I6)
99998 FORMAT (1X,2I10)
99997 FORMAT (2X, I4, 2(2X, E12.6))
99996 FORMAT (1X,414)
99995 FORMAT (2(2X,E12.6))
99994 FORMAT (1X,4I10)
      END
      real FUNCTION FBND(I,X,Y,RUSER,IUSER)
      .. Scalar Arguments ..
      real
      INTEGER
                         I
      .. Array Arguments ..
                          RUSER(*)
```

```
INTEGER
                   IUSER(*)
.. Local Scalars ..
real
                   RADIUS2, XO, XA, XB, YO
.. Executable Statements ..
XA = RUSER(1)
XB = RUSER(2)
XO = RUSER(3)
YO = RUSER(4)
FBND = 0.e0
IF (I.EQ.1) THEN
line 1,2,3, and 4: ellipse centred in (XO,YO) with
XA and XB as coefficients
   FBND = ((X-X0)/XA)**2 + ((Y-Y0)/XB)**2 - 1.e0
ELSE IF (I.EQ.2) THEN
line 24, 27, 33 and 38 are a circle centred in (XO,YO)
with radius SQRT(RADIUS2)
   x0 = 20.5e0
   YO = 4.e0
   RADIUS2 = 4.25e0
   FBND = (X-X0)**2 + (Y-Y0)**2 - RADIUS2
ELSE IF (I.EQ.3) THEN
   X0 = 17.e0
   Y0 = 8.5e0
   RADIUS2 = 5.e0
   FBND = (X-X0)**2 + (Y-Y0)**2 - RADIUS2
ELSE IF (I.EQ.4) THEN
  X0 = 17.e0
   y0 = 8.5e0
   RADIUS2 = 5.e0
   FBND = (X-X0)**2 + (Y-Y0)**2 - RADIUS2
ELSE IF (I.EQ.5) THEN
   X0 = 19.5e0
   Y0 = 4.e0
   RADIUS2 = 1.25e0
   FBND = (X-X0)**2 + (Y-Y0)**2 - RADIUS2
END IF
RETURN
END
```

9.2 Program Data

```
D06BAF Example Program Data
40
                                                                      :NLINES (m)
                      9.5000 -14.0000 -4.0000 -2.0000
  9.5000 33.0000
                                                                 2.0000
           2.0000 -2.0000 -4.0000 -2.0000
  4.0000
                                                      2.0000 4.0000
  7.0000
           9.0000 13.0000 16.0000
                                           9.0000 12.0000 7.0000

      10.0000
      18.0000
      21.0000
      17.0000
      20.0000
      16.0000
      20.0000

      15.5000
      16.0000
      18.0000
      21.0000
      16.0000
      18.0000
      18.5811

      21.0000
      17.0000
      20.5000
      23.0000
      :(COORCH

                                                                :(COORCH(1,1:m))
           7.5000 16.0000
                                 7.5000
                                                      3.0000 3.0000
 -1.0000
                                            3.0000
           7.0000 8.0000 12.0000 12.0000 12.0000 12.0000
  3.0000
           3.0000
2.0000
                       3.0000 3.0000
  3.0000
                                            5.0000
                                                       5.0000 12.0000
 12.0000
                       2.0000
                                  3.0000
                                             3.0000
                                                        5.0000
                                                                  5.0000
           6.0000
                      6.0000 6.0000
                                           6.5000
                                                      6.5000 10.0811
  6.0000
 10.0811 10.7361 10.7361 12.0000 12.0000
                                                                :(COORCH(2,1:m))
                      3.3333 2.6667
3.0000 3.0000
 -2.6667 -3.3333
                                                                :(COORUS(1,1:4))
  3.0000
           3.0000
                                                                :(COORUS(2,1:4))
15 1 2 1 0.9500 15 2 3 1
                                            1.0500
15 3 4 1
                0.9500
                          15 4 1 1
                                            1.0500
 4 6 5 -1
              1.0000
                         10 10 6 0
                                            1.0000
                         4 8 7 -3
4 13 14 0
    7 10 0
                1.0000
10
                                            1.0000
15 14 8 0
                                          1.0000
               1.0000
```

D06BAF.10 [NP3546/20A]

```
10 9 13 0
            1.0000
                    10 12 9 0 1.0000
4 11 12 0
            1.0000 15 5 11 0 1.0000
            1.0000
4 16 15
                    7 19 16 0 1.0000
7 17 20 0 1.0000
         Ω
4 20 19
         0
             1.0000
                    13 22 18
4 18 17
             1.0000
         0
                              0
                                   1.0000
5 21 22
            1.0000
                    13 15 21
         0
                              0 1.0000
4 24 23
            1.0000
                    10 24 32
                              2 1.0000
         0
                    4 34 31
4 36 35
4 31 32
         0
             1.0000
                              0
                                   1.0000
10 34 35
         3
             1.0000
                              0
                                   1.0000
4 40 36
         0
            1.0000
                     4 39 40 0 1.0000
4 38 39
         0
            1.0000
                    4 37 38 0 1.0000
10 37 33
         4
             1.0000
                    4 30 33
                              0
                                  1.0000
                      4 27 29
4 29 30
         0
             1.0000
                              0
                                   1.0000
4 28 27 0
                    10 26 28 5
            1.0000
                                   1.0000
4 25 26 0
            1.0000
                    4 23 25 0
                                   1.0000 :(LINE(:,j),RATE(j),j=1,m)
                                      :NCOMP (n, number of contours)
                                      :number of lines in contour 1
  2 3 4
                                                :lines of contour 1
1
                                       :number of lines in contour 2
10
14 13 12 11 10 9 8 7 6 5
                                                :lines of contour 2
8
                                      :number of lines in contour 3
22 21 20 19 18 17 16 15
                                                :lines of contour 3
                                      :number of lines in contour 4
18
30 29 28 27 26 25 24 23 40 39
38 37 36 35 34 33 32 31
                                                :lines of contour 4
'N'
                                         :Printing option 'Y' or 'N'
```

9.3 Program Results

D06BAF Example Program Results

```
ANALYSIS OF THE BOUNDARY CREATED:
THE BOUNDARY MESH CONTAINS 259 VERTEX AND
                                             259 EDGES
THERE ARE
              4 COMPONENTS CONNECTED THE BOUNDARY
THE 1-st COMPONENT CONTAINS 4 LINES IN ANTICLOCKWISE ORIENTATION
THE 2-nd COMPONENT CONTAINS
                               10 LINES IN CLOCKWISE ORIENTATION
                               8 LINES IN CLOCKWISE ORIENTATION
THE 3-rd COMPONENT CONTAINS
                               18 LINES IN CLOCKWISE ORIENTATION
THE 4-th COMPONENT CONTAINS
Boundary mesh characteristics
        259
NEDGE =
         259
Complete mesh (via the 2D Delaunay-Voronoi mesh
generator) characteristics
NV = 652
NELT = 1049
Complete mesh (via the 2D Advancing front mesh
generator) characteristics
NV = 662
NELT = 1069
```

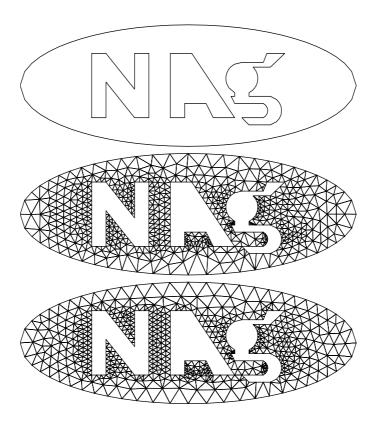


Figure 1
The boundary mesh (top), the Delaunay-Voronoi mesh (middle) and the Advancing Front mesh (bottom) of the NAG logo geometry

D06BAF.12 (last) [NP3546/20A]