NAG Fortran Library Routine Document

D02PYF

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of **bold italicised** terms and other implementation-dependent details.

1   Purpose

D02PYF provides details about an integration performed by either D02PCF or D02PDF.

2   Specification

```
SUBROUTINE D02PYF(TOTFCN, STPCST, WASTE, STPSOK, HNEXT, IFAIL)
INTEGER          TOTFCN, STPCST, STPSOK, IFAIL
real             WASTE, HNEXT
```

3   Description

D02PYF and its associated routines (D02PCF, D02PDF, D02PVF, D02PWF, D02PXF, D02PZF) solve the initial value problem for a first-order system of ordinary differential equations. The routines, based on Runge–Kutta methods and derived from RKSUITE (Brankin *et al.* (1991)), integrate

$$y' = f(t, y) \quad \text{given} \quad y(t_0) = y_0$$

where y is the vector of n solution components and t is the independent variable.

After a call to D02PCF or D02PDF, D02PYF can be called to obtain information about the cost of the integration and the size of the next step.

4   References

Brankin R W, Gladwell I and Shampine L F (1991) RKSUITE: A suite of Runge–Kutta codes for the initial value problems for ODEs *SoftReport 91-S1* Southern Methodist University, Dallas

5   Parameters

1:    TOTFCN – INTEGER   *Output*

On exit: the total number of evaluations of f used in the primary integration so far; this does not include evaluations of f for the secondary integration specified by a prior call to D02PVF with ERRASS = .TRUE..

2:    STPCST – INTEGER   *Output*

On exit: the cost in terms of number of evaluations of f of a typical step with the method being used for the integration. The method is specified by the parameter METHOD in a prior call to D02PVF.

3:    WASTE – **real**   *Output*

On exit: the number of attempted steps that failed to meet the local error requirement divided by the total number of steps attempted so far in the integration. A 'large' fraction indicates that the integrator is having trouble with the problem being solved. This can happen when the problem is 'stiff' and also when the solution has discontinuities in a low-order derivative.

4:    STPSOK – INTEGER   *Output*

On exit: the number of accepted steps.

5:     HNEXT – **real**   *Output*

    On exit: the step size the integrator will attempt to use for the next step.

6:     IFAIL – INTEGER   *Input/Output*

    On entry: IFAIL must be set to 0, -1 or 1. Users who are unfamiliar with this parameter should refer to Chapter P01 for details.

    On exit: IFAIL = 0 unless the routine detects an error (see Section 6).

    For environments where it might be inappropriate to halt program execution when an error is detected, the value -1 or 1 is recommended. If the output of error messages is undesirable, then the value 1 is recommended. Otherwise, for users not familiar with this parameter the recommended value is 0. **When the value -1 or 1 is used it is essential to test the value of IFAIL on exit.**

6   Error Indicators and Warnings

If on entry IFAIL = 0 or -1, explanatory error messages are output on the current error message unit (as defined by X04AAF).

Errors or warnings detected by the routine:

IFAIL = 1

    An invalid call to D02PYF has been made, for example without a previous call to D02PCF or D02PDF. If on entry IFAIL=0 or -1, the precise form of the error will be detailed on the current error message unit (as defined by X04AAF). You cannot continue integrating the problem.

7   Accuracy

Not applicable.

8   Further Comments

When a secondary integration has taken place, that is when global error assessment has been specified using ERRASS = .TRUE. in a prior call to D02PVF, then the approximate extra number of evaluations of f used is given by $2 \times$ STPSOK $\times$ STPCST for METHOD = 2 or 3 and $3 \times$ STPSOK $\times$ STPCST for METHOD = 1.

9   Example

See Section 9 of the documents for D02PCF, D02PDF, D02PWF, D02PXF and D02PZF.